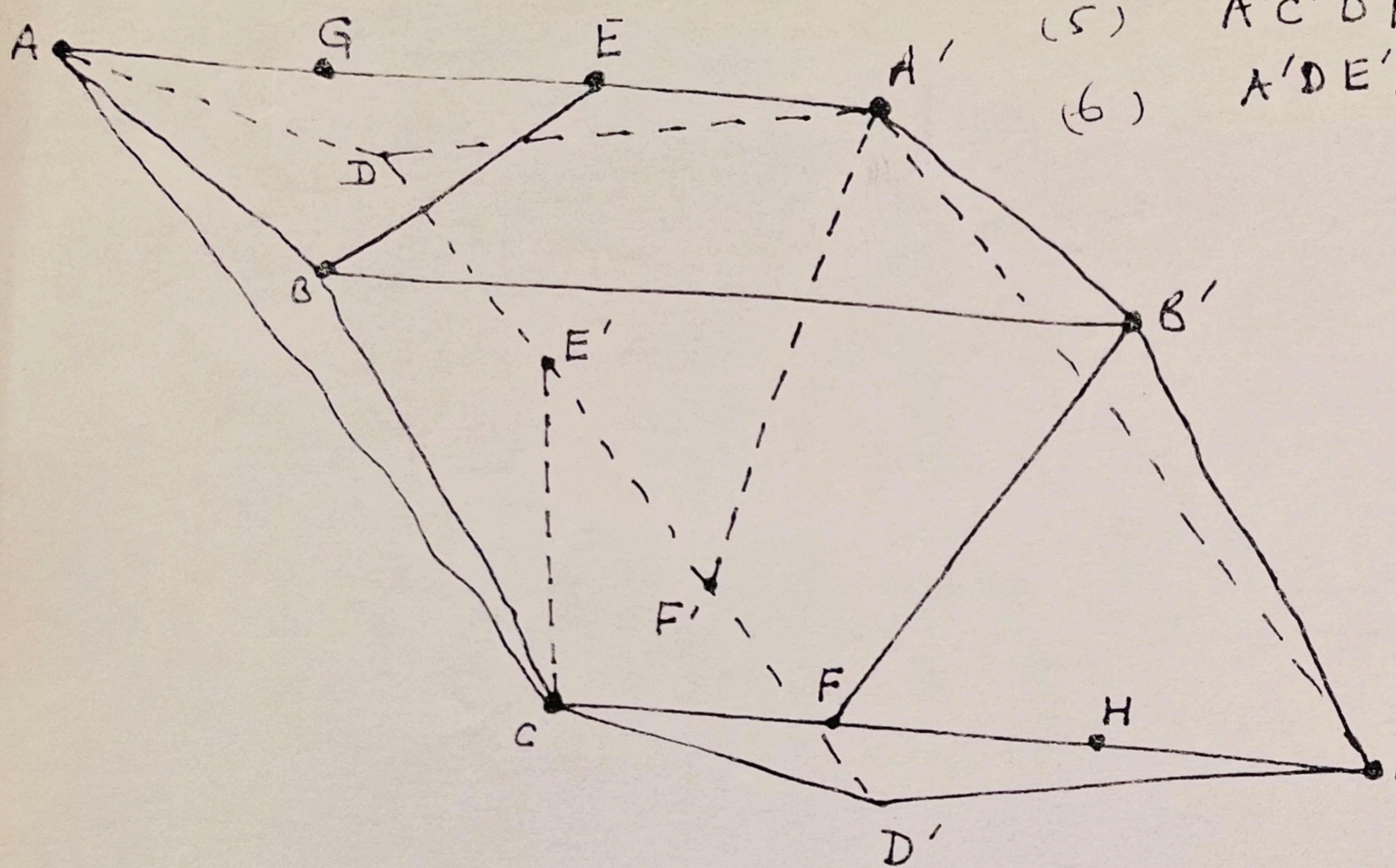


$\mathbb{R}^3$  space obtained  
 an interesting euclidean  
 by identification of  
 face pairs (1) - (6)

no. of 3-cells  $f_3 = 1$   
 no. of 2-cells  $f_2 = 6$  :

- (1)  $ABC = A'B'C'$
- (2)  $AGEA'D = CFHC'D'$
- (3)  $ADE'C = BEA'B'$
- (4)  $E'F'D'C = AGE B$
- (5)  $A'C'D'F' = BB'FC$
- (6)  $A'DE'F' = B'FHC'$



no. of 1-cells  $f_1 = 6$ :

- (i)  $AC = A'C' = BB'$
- (ii)  $BC = B'C' = A'F'$
- (iii)  $AB = A'B' = E'C$
- (iv)  $CD' = AD = BE$
- (v)  $D'C' = DA' = FB'$
- (vi)  $CF = F'D' = GE = FH = DE'$

$\leftarrow EA' = HC' = E'F' = AG$

see char =  $f_0 - f_1 + f_2 - f_3 = 0$ . So  $M^3$  is a  
 closed 3-mfld

no. of 0-cells  $f_0 = 1$ :

$A = A' = B = B' = E' = C = C' = F' = F$   
 $= D = D' = E = G = H$

Incidence : (oriented)

2 cells  
 3 cells  $[0 \ 0 \ 0 \ 0 \ 0 \ 0]$

1 cells  
 $\begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$

	1-cells	(i)	(ii)	(iii)	(iv)	(v)	(vi)
2 cells		(i)	(ii)	(iii)	(iv)	(v)	(vi)
(1)		-1	1	1			
(2)		1			-1	-1	3
(3)		-1		1	1		1
(4)				-1	-1	1	2
(5)		1	-1			-1	-1
(6)			-1			-1	2

eqvt.  $\begin{bmatrix} 5 & 0 \\ 0 & 1 \\ & & 5 \end{bmatrix}$   
 (over  $\mathbb{Z}$ )

$H_2(M^3) \cong 0$

$\mathbb{Z} \leftarrow \mathbb{Z} \xrightarrow{5} \mathbb{Z} \xrightarrow{5} \mathbb{Z} \xrightarrow{5} \mathbb{Z}$

So homology is that of 3-sphere?  $H_0(M^3) \cong H_3(M^3) \cong \mathbb{Z}$   
 $H_1(M^3) \cong \mathbb{Z}/5$

Is  $M^3 \cong S^3$  or is  $M^3$  a homology 3-sphere with  $\pi_1 \neq \mathbb{Z}$ ?

Calculate  $\pi_1$  to see...

Maybe  $M^3$  is a lens space?

as Prof. Dauter: as above shows it is possible  
 that one may obtain interesting 3-manifolds  
 - you euclidean  
 K. S. Sarkar  
 13.3.95